Math 4329, Test II

Name _____

1. a. A table of values for f(x) is:

x	f(x)
0.0	0.0
0.1	3.0
0.2	0.0

Use quadratic interpolation to estimate f(0.05).

b. If $f(x) = 3 \sin(5\pi x)$, obtain a reasonable bound on the error in your estimate of f(0.05).

2. Use Taylor series expansions to determine the error in the approximation $u''(t) \approx \frac{u(t)-2u(t-h)+u(t-2h)}{h^2}$

3. The following function is a cubic spline for what values of a, b, c?

$$s(x) = 2x^3 - 3x^2 + 3x - 4 \quad for \quad 0 < x \le 1 \\ = x^3 + ax^2 + bx + c \quad for \quad 1 < x \le 2$$

4. Determine values for A, B, C which make

$$\int_0^h f(x) dx \approx Ahf(0) + Bhf(h/3) + Chf(h)$$

as high order as possible. What is the degree of precision and what is the global order?

- 5. a. If a quadrature rule yields errors of 0.0064 when h = 0.01 and 0.0002 when h = 0.0025, what is the experimental order? $(O(h^2))$
 - b. Of all quadrature rules with n sample points per strip, the one with highest degree of precision is called what?
 - c. Gaussian elimination, when applied to a general N by N linear system, requires approximately how many multiplications?
 - d. The strategy of switching rows during Gaussian elimination to always bring the largest (in absolute value) potential pivot to the diagonal is called what?
 - e. True or False: If f(x) is a smooth function and $L_n(x)$ is the Lagrange polynomial that interpolates to f at uniformly spaced points $a = x_0, x_1, ..., x_n = b$, then for all a < x < b, $L_n(x)$ is guaranteed to converge to f(x) as $n \to \infty$. (Assume no roundoff error.)