Math 4370 Dr. Duval

## COMBINATORICS Homework

Thursday, February 16

Follow the separate general guidelines for Parts A,B,C. Be sure to include and label *all* four standard parts (a), (b), (c), (d) of Part A in what you hand in.

## Nonincreasing finite sequences of integers (and some Ferrers shapes)

Subsection 2.3.1 (and Subsection 2.3.2 up to and including Example 2.23)

## A: Reading questions. Due by 3pm, Mon., 27 Feb.

- 1. What is the difference between a **partition** of an integer, and a **composition** of that integer? What is the difference between a partition of an **integer** and a partition of a **set**?
- 2. Verify the entries for p(5) and p(6) in Figure 2.4 by explicitly listing partitions. (This is similar to Example 2.20.)
- 3. What does  $p_k(n)$  count? Compute  $p_3(6)$  by explicitly listing partitions.
- 4. Translate the rule for partitions of integers into a rule for Ferrers shapes: Describe a rule for how you are allowed to arrange the boxes in a Ferrers shape without using the language of partitions. What sort of arrangement of boxes is **not** allowed in a Ferrers shape?
- 5. Draw the Ferrers shape for the partition (6, 4, 3, 1) and use this shape to find the conjugate of the partition.
- B: Warmup exercises. For you to present in class. Due by the end of class Tue., 28 Feb.
  - 1. 2.10 Supplementary Exercise: 16, 17, 18, 20