Math 4303 Dr. Duval

# FUNDAMENTALS OF MATH

Homework

#### Thursday, August 29

Follow the separate general guidelines for Parts A,B,C. Be sure to include and label *all* four standard parts (a), (b), (c), (d) of Part A in what you hand in.

## Periodic decimals

Section 2.1.3 (and last two pages of section 2.1.2)

A: Reading questions. Due by 3pm, Wed., 4 Sep.

- 1. Why doesn't the proof of Theorem 2.4 actually prove that the period of the repeating decimal of a/b equals b-1 instead of merely being at most b-1?
- 2. Give three more examples of each of the types of decimals in Table 3.
- 3. Can you use a calculator to find the period of a repeating decimal? Can you do it always? Explain.
- 4. Theorems 2.5 and 2.6 both describe the rational number form of a terminating decimal. What is the difference between these two theorems? Why would we want more than one theorem like this? (In other words, why state both theorems?)
- 5. Represent  $0.\overline{915}$  as a fraction. Show your calculations. Which theorem in the text addresses an expression of this form?

**B:** Warmup exercises. For you to present in class. Due by end of class Thu., 5 Sep.

**2.1.3 Problems:** 1, 2, 5, 8

# The distribution of various types of numbers Section 2.1.4

### A: Reading questions. Due by 3pm, Mon., 9 Sep.

- 1. "Question 1" on p. 41 is answered at the end of the section on p. 47. Which number is the irrational one? How do you know it's irrational?
- 2. Give an example of a number that is algebraic but not rational. How do you know it is algebraic? How do you know it is not rational?
- 3. What is a transcendental number? Give two examples. (You don't have to prove your answer is correct, but you can give a reference from the text.)
- 4. What does it mean for a set to be countable? Give an example of a set that is not countable, and an example of a set that is countably infinite. (Don't use the examples in the following Reading Question.)
- 5. The rational numbers are countably infinite, and the real numbers are not countable. What does this mean about how likely you are to get a rational number if you pick a real number at random? Are there more rational numbers or more irrational numbers?
- B: Warmup exercises. For you to present in class. Due by the end of class Tue., 10 Sep.
  2.1.4 Problems: 1, 2, 3, 4, 5ab, 8a