Homework 9

due Thursday, November 9

1. Let D be the relation on \mathbb{R} defined by x D y if $x-y \in \mathbb{Z}$. Prove that D is an equivalence relation. Describe the elements of the equivalence class 23/17.

2. Prove that

$$\{M_r \colon r \in \mathbb{R}, r \ge 0\}$$

is a partition of \mathbb{C} , the set of complex numbers, where each

$$M_r = \{ z \in \mathbb{C} \colon ||z|| = r \}.$$

[Notes about complex numbers: A complex number is of the form z = x + iy, where x and y are real, and $i = \sqrt{-1}$ is the imaginary unit. The magnitude of a complex number z = x + iy is $||z|| = \sqrt{x^2 + y^2}$.]